

**ECUACIÓN GENERAL DE 2º GRADO:**

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Propiedades de los logaritmos:

$$\log(ab) = \log a + \log b$$

$$\log\left(\frac{a}{b}\right) = \log a - \log b$$

$$\log a^n = n \log a \quad \log^n \sqrt{a} = \frac{1}{n} \log a$$

Identidades Trigonómicas:

$$\sin^2 \alpha + \cos^2 \alpha = 1 \quad \cot \alpha = \frac{\cos \alpha}{\sin \alpha}$$

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha} \quad \cot = \frac{1}{\tan \alpha}$$

$$\sec \alpha = \frac{1}{\cos \alpha} \quad \csc \alpha = \frac{1}{\sin \alpha}$$

$$\sec^2 \alpha = 1 + \tan^2 \alpha \quad \csc^2 \alpha = 1 + \cot^2 \alpha$$

**GEOMETRÍA ANALÍTICA**

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

Pendiente:

$$m = \frac{y_1 - y_2}{x_1 - x_2}$$

Punto Medio:

$$x = \frac{x_1 + x_2}{2} \quad y = \frac{y_1 + y_2}{2}$$

División de Segmentos:

$$x = \frac{x_1 + rx_2}{1+r} \quad y = \frac{y_1 + ry_2}{1+r}$$

Ángulo entre dos Rectas:

$$\tan \theta_1 = \frac{m_2 - m_1}{1 + m_2 m_1} \quad \tan \theta_2 = \frac{m_1 - m_2}{1 + m_1 m_2}$$

**ECUACIONES DE LA RECTA:**

$$y - y_1 = m(x - x_1)$$

$$y - y_1 = \frac{y_1 - y_2}{x_1 - x_2}(x - x_1)$$

$$y = mx + b$$

$$\frac{x}{a} + \frac{y}{b} = 1$$

Distancia de un punto a una recta:

$$d = \frac{|Ax + By + c|}{\pm \sqrt{A^2 + B^2}}$$

**ECUACIONES DE LA CIRCUNFERENCIA:**

$$x^2 + y^2 = r^2 \quad \text{Centro en el origen.}$$

$$(x - h)^2 + (y - k)^2 = r^2 \quad \text{Centro en (h,k)}$$

$$Ax^2 + By^2 + Dx + Ey + F = 0$$

$A = B$  y del mismo signo

**ECUACIONES DE LA PARÁBOLA:**

$$y^2 = 4px \quad x^2 = 4py \quad \text{Vértice en el origen.}$$

$$(y - k)^2 = 4p(x - h) \quad \text{Vértice en (h,k)}$$

$$(x - h)^2 = 4p(y - k)$$

$$Ax^2 + Dx + Ey + F = 0$$

$$By^2 + Dx + Ey + F = 0$$

Long. Lado recto = 4p.

**ECUACIONES DE LA ELIPSE:**

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1; \quad \frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$$

$$\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$$

$$\frac{(x - h)^2}{b^2} + \frac{(y - k)^2}{a^2} = 1$$

$$\text{Long. Lado recto} = \frac{2b^2}{a} \quad c^2 = a^2 - b^2$$

Excentricidad:

$$e = \frac{c}{a} = \frac{\sqrt{a^2 - b^2}}{a}$$

**ECUACIONES DE LA HIPÉRBOLA:**

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad \frac{y^2}{a^2} - \frac{x^2}{b^2} = 1$$

$$\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1$$

$$\frac{(y - k)^2}{a^2} - \frac{(x - h)^2}{b^2} = 1$$

$$\text{Long. Lado recto} = \frac{2b^2}{a} \quad e = \frac{c}{a}$$

**FÓRMULAS PARA DERIVACIÓN:**

$$\frac{d}{dx}(c) = 0; \quad \frac{d}{dx}(x) = 1;$$

$$\frac{d}{dx}(cv) = c \frac{d(v)}{dx}$$

$$\frac{d}{dx}(u + v - w) = \frac{d(u)}{dx} + \frac{d(v)}{dx} - \frac{d(w)}{dx}$$

$$\frac{d}{dx}(v^n) = n(v)^{n-1} \frac{d(v)}{dx}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v \frac{d(u)}{dx} - u \frac{d(v)}{dx}}{v^2}$$

$$\frac{d}{dx}\left(\frac{u}{c}\right) = \frac{d(u)}{c}$$

$$\frac{d}{dx}(y) = \frac{d(y)}{dv} \cdot \frac{d(v)}{dx}; \text{ siendo } y \text{ función de } v$$

$$\frac{dy}{dx} = \frac{1}{\frac{dx}{dy}}; \text{ siendo } y \text{ función de } x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x} \frac{d(x)}{dx}$$

$$\frac{dv}{dx}(\operatorname{arcsec} v) = \frac{\frac{dv}{dx}}{v\sqrt{v^2-1}}$$

$$\frac{d}{dx}(\log v) = \frac{\log e}{v} \frac{dv}{dx}$$

$$\frac{d}{dx}(a^v) = a^v \ln a \frac{dv}{dx}$$

$$\frac{d}{dx}(e^v) = e^v \frac{dv}{dx}$$

$$\frac{d}{dx}(u^v) = v u^{v-1} \frac{du}{dx} + \ln u \cdot u^v \frac{dv}{dx}$$

$$\frac{d}{dx}(\operatorname{sen} v) = \cos v \frac{dv}{dx}$$

$$\frac{d}{dx}(\cos v) = -\operatorname{sen} v \frac{dv}{dx}$$

$$\frac{d}{dx}(\operatorname{tg} v) = \sec^2 v \frac{dv}{dx} \quad \frac{d}{dx}(\operatorname{ctg} v) = -\operatorname{csc}^2 v \frac{dv}{dx}$$

$$\frac{d}{dx}(\sec v) = \sec v \operatorname{tg} v \frac{dv}{dx}$$

$$\frac{d}{dx}(\operatorname{csc} v) = -\operatorname{csc} v \operatorname{ctg} v \frac{dv}{dx}$$

$$\frac{d}{dx} \operatorname{vers} v = \operatorname{sen} v \frac{dv}{dx} \quad \frac{d}{dx}(\operatorname{arcsen} v) = \frac{\frac{dv}{dx}}{\sqrt{1-v^2}}$$

$$\frac{d}{dx}(\operatorname{arccos} v) = -\frac{\frac{dv}{dx}}{\sqrt{1-v^2}}$$

$$\frac{d}{dx}(\operatorname{arctg} v) = \frac{\frac{dv}{dx}}{1+v^2}$$

$$\frac{dv}{dx}(\operatorname{arcsec} v) = \frac{\frac{dv}{dx}}{v\sqrt{v^2-1}}$$

$$\frac{d}{dx}(\operatorname{arc} \operatorname{csc} v) = -\frac{\frac{dv}{dx}}{v\sqrt{v^2-1}}$$

$$\frac{d}{dx}(\operatorname{arc} \operatorname{vers} v) = \frac{\frac{dv}{dx}}{\sqrt{2v-v^2}}$$

FÓRMULA DE INTEGRACIÓN:

$$\int du + dv - dw = \int du + \int dv - \int dw$$

$$\int a dv = a \int dv$$

$$\int dx = x + c$$

$$\int v^n dv = \frac{v^{n+1}}{n+1} + c$$

$$\int \frac{dv}{v} = \ln v + c$$

$$\int a^v dv = \frac{a^v}{\ln a} + C$$

$$\int e^v dv = e^v + C$$

$$\int \operatorname{sen} v dv = -\cos v + C$$

$$\int \cos v dv = \operatorname{sen} v + C$$

$$\int \sec^2 v dv = \operatorname{tg} v + C$$

$$\int \operatorname{csc}^2 v dv = -\operatorname{ctg} v + C$$

$$\int \sec v \operatorname{tg} v dv = \sec v + C$$

$$\int \operatorname{csc} v \operatorname{ctg} v dv = -\operatorname{csc} v + C$$

$$\int \operatorname{tg} v dv = -\ln |\cos v| + C = \ln |\operatorname{sen} v| + C$$

$$\int \operatorname{ctg} v dv = \ln |\operatorname{sen} v| + C$$

$$\int \sec v dv = \ln |\sec v + \operatorname{tg} v| + C$$

$$\int \operatorname{csc} v dv = \ln |\operatorname{csc} v - \operatorname{ctg} v| + C$$

$$\int \frac{dv}{v^2+a^2} = \frac{1}{a} \operatorname{arctan} \frac{v}{a} + C$$

$$\int \frac{dv}{v^2-a^2} = \frac{1}{2a} \ln \left| \frac{v-a}{v+a} \right| + C$$

$$\int \frac{dv}{a^2-v^2} = \frac{1}{2a} \ln \left| \frac{a+v}{a-v} \right| + C$$

$$\int \frac{dv}{\sqrt{a^2-v^2}} = \operatorname{arcsen} \frac{v}{a} + C$$

$$\int \frac{dv}{\sqrt{v^2 \pm a^2}} = \ln \left| v + \sqrt{v^2 \pm a^2} \right| + C$$

$$\int \sqrt{a^2-v^2} dv = \frac{v}{2} \sqrt{a^2-v^2} + \frac{a^2}{2} \operatorname{arcsen} \frac{v}{a} + C$$

$$\int \sqrt{v^2 \pm a^2} dv = \frac{v}{2} \sqrt{v^2 \pm a^2} \pm \frac{a^2}{2} \ln \left| v + \sqrt{v^2 \pm a^2} \right| + C$$